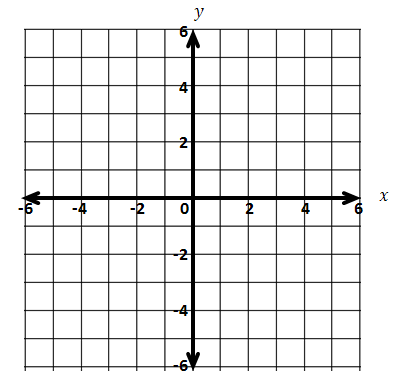
Lesson 16: Graphs Can Solve Equations Too

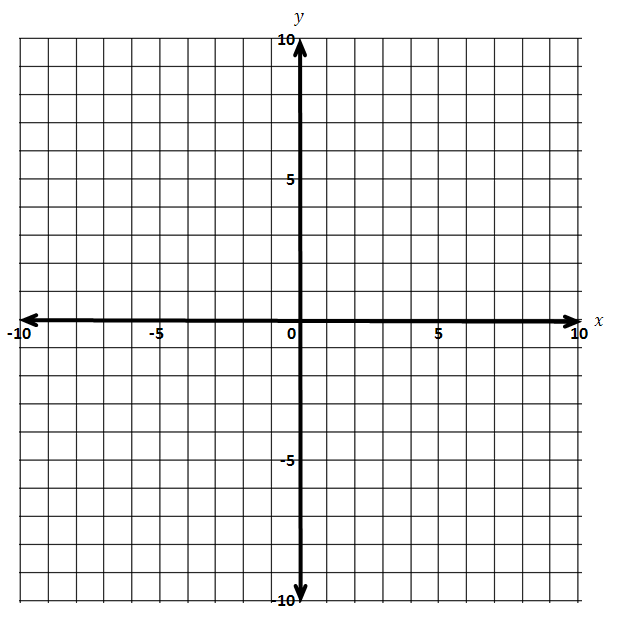
Classwork

Opening Exercise

1. Solve for in the following equation:



1. Now let and . When does ? To answer this, first graph and on the same set of axes.
2. When does ? What is the visual significance of the points where ?
3. Is each intersection point an element of the graph and an element of the graph of ? In other words, do the functions and really have the same value when ? What about when ?

****Example 1

Solve this equation by graphing two functions on the same Cartesian plane:

Let and let where can be any real number.

We are looking for values of at which the functions and have the same output value.

Therefore, we set and so we can plot the graphs on the same coordinate plane:

From the graph, we see that the two intersection points are

\_\_\_\_\_\_\_\_\_\_\_\_\_ and \_\_\_\_\_\_\_\_\_\_\_\_\_.

The fact that the graphs of the functions meet at these two points means that when is \_\_\_\_\_\_\_ both and are \_\_\_\_\_\_\_, or when is \_\_\_\_\_\_\_ both and are \_\_\_\_\_\_\_.

Thus, the expressions and are equal when \_\_\_\_\_\_\_ or when \_\_\_\_\_\_\_.

Therefore, the solution set to the original equation is \_\_\_\_\_\_\_\_\_\_\_.



Example 2

Solve this equation graphically:

* 1. Write the two functions represented by each side of the equation.
  2. Graph the functions in an appropriate viewing window.
  3. Determine the intersection points of the two functions.
  4. Verify that the -coordinates of the intersection points are solutions to the equation.

Exercises 1-5

Use graphs to find approximate values of the solution set for each equation. Use technology to support your work. Explain how each of your solutions relates to the graph. Check your solutions using the equation.

1.  2.

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1. The graphs of the functions and are shown.
   1. Use the graph to *approximate* the solution(s) to the equation
   2. Let and let . Find *all* solutions to the equation . Verify any exact solutions that you determine using the definitions of *f* and *g*. Explain how you arrived at your solutions.
2. The graphs of , a function that involves taking an absolute value, and a linear function, are shown to the right. Both functions are defined over all real values for Tami concluded that the equation has no solution.

Do you agree or disagree? Explain your reasoning.



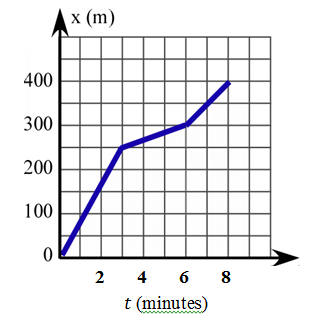
1. The graphs of (a function that involves taking the absolute value) and (an exponential function) are shown below. Sharon said the solution set to the equation ) is exactly

Do you agree or disagree with Sharon? Explain your reasoning.

Problem Set

1. Solve the following equations graphically. Verify the solution set using the original equations.

In each exercise, the graphs of the functions and are shown on the same Cartesian plane. Estimate the solution set to the equation . Assume that the graphs of the two functions only intersect at the points shown on the graph.

1.  3.
2.  5.
3. The graph below shows Glenn’s distance from home as he rode his bicycle to school, which is just down his street. His next-door neighbor Pablo, who lives 100 m closer to the school, leaves his house at the same time as Glenn. He walks at a constant velocity and they both arrive at school at the same time.
   1. Graph a linear function that represents Pablo’s distance from Glenn’s home as a function of time.
   2. Estimate when the two boys pass each other.
   3. Write piecewise-linear functions to represent each boy’s distance and use them to verify your answer to part (b).